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Scrivi l'equazione della circonferenza passante per l'origine e tangente in $A(1; 2)$ alla retta di equazione
 $y = -3x + 5$

$$[x^2 + y^2 + x - 3y = 0]$$

$$x^2 + y^2 + ax + by + c = 0$$

$$\begin{aligned} O(0,0) \rightarrow & \left\{ \begin{array}{l} c = 0 \\ a + b = 0 \end{array} \right. \\ A(1,2) \rightarrow & \left\{ \begin{array}{l} c = 0 \\ 1 + 4 + a + 2b = 0 \end{array} \right. \Rightarrow a = -2b - 5 \end{aligned}$$

$$\begin{cases} x^2 + y^2 + ax + by = 0 \\ y = -3x + 5 \end{cases}$$

$$x^2 + (-3x + 5)^2 + ax + b(-3x + 5) = 0$$

$$x^2 + 9x^2 + 25 - 30x + ax - 3bx + 5b = 0$$

$$10x^2 + (a - 30 - 3b)x + 25 + 5b = 0$$

$$\Delta = 0 \quad (a - 30 - 3b)^2 - 40(25 + 5b) = 0$$

\uparrow
 $-2b - 5$

$$\begin{aligned} (-5b - 35)^2 - 1000 - 200b &= 0 \\ \downarrow \\ [(-5)(b+7)]^2 & \end{aligned}$$

$$25(b^2 + 49 + 14b) - 1000 - 200b = 0$$

$$b^2 + 49 + 14b - 40 - 8b = 0$$

$$b^2 + 6b + 9 = 0 \quad (b+3)^2 = 0 \Rightarrow b = -3$$

$$\begin{cases} a = -2b - 5 = 6 - 5 = 1 \\ b = -3 \\ c = 0 \end{cases}$$

$$\boxed{x^2 + y^2 + x - 3y = 0}$$

Dato il triangolo di vertici $A(1; 2)$, $B(-7; 6)$ e $C(-1; 0)$, determina l'equazione della circonferenza circoscritta e quella della circonferenza con centro in C e tangente alla retta AB .

$$\begin{aligned} & [x^2 + y^2 + 6x - 8y + 5 = 0; \\ & \quad 5x^2 + 5y^2 + 10x - 31 = 0] \end{aligned}$$

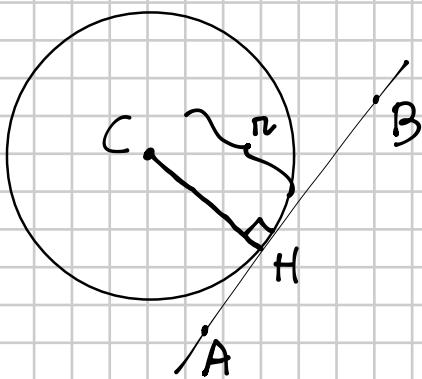
$$x^2 + y^2 + ax + by + c = 0$$

$$\begin{array}{l} A \\ B \\ C \end{array} \left\{ \begin{array}{l} 1+4+a+2b+c=0 \\ 49+36-7a+6b+c=0 \\ 1-a+c=0 \end{array} \right. \quad \left\{ \begin{array}{l} 5+a+2b+a-1=0 \\ 85-7a+6b+a-1=0 \\ c=a-1 \end{array} \right.$$

$$\left\{ \begin{array}{l} 2a+2b=-4 \rightarrow a+b=-2 \\ -6a+6b=-84 \rightarrow -a+b=-14 \\ // \end{array} \right. \quad \left\{ \begin{array}{l} a=-b-2 \\ b+2+b=-14 \\ // \end{array} \right.$$

$$\left\{ \begin{array}{l} 2b=-16 \Rightarrow \begin{cases} a=6 \\ b=-8 \end{cases} \\ c=5 \end{array} \right.$$

$$\boxed{x^2 + y^2 + 6x - 8y + 5 = 0}$$



$$A(1, 2) \quad B(-7, 6)$$

$$\frac{y-2}{6-2} = \frac{x-1}{-7-1}$$

$$\frac{y-2}{4} = \frac{x-1}{-8-2}$$

$$-2y + 4 = x - 1 \quad x + 2y - 5 = 0$$

$$r = d(C, AB) = \frac{|-1+2 \cdot 0 - 5|}{\sqrt{1^2 + 2^2}} = \frac{6}{\sqrt{5}}$$

Circ.

$$(x+1)^2 + (y-0)^2 = \frac{36}{5}$$

$$x^2 + 1 + 2x + y^2 - \frac{36}{5} = 0$$

$$\boxed{5x^2 + 5y^2 + 10x - 31 = 0}$$

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$$x^2 + y^2 + |2x - 2| + 4y = 0$$

Rappresentare graficamente

$$2x - 2 \geq 0 \Rightarrow |2x - 2| = 2x - 2$$

$$x \geq 1$$

$$2x - 2 < 0 \Rightarrow |2x - 2| = -2x + 2$$

$$x < 1$$

$$\begin{cases} x^2 + y^2 + 2x - 2 + 4y = 0 & \text{se } x \geq 1 \\ x^2 + y^2 - 2x + 2 + 4y = 0 & \text{se } x < 1 \end{cases}$$

$$\textcircled{1} \quad \begin{cases} x^2 + y^2 + 2x + 4y - 2 = 0 & \text{se } x \geq 1 \end{cases}$$

$$\textcircled{2} \quad \begin{cases} x^2 + y^2 - 2x + 4y + 2 = 0 & \text{se } x < 1 \end{cases}$$

$$\textcircled{1} \quad C_1(-1, -2) \quad r_1 = \sqrt{1+4+2} = \sqrt{7}$$

$$\textcircled{2} \quad C_2(1, -2) \quad r_2 = \sqrt{1+4-2} = \sqrt{3}$$

